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Hybrid finite-element/molecular-dynamics/ electronic-density-functional approach to materials simulations on parallel computers

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Abstract

A hybrid simulation approach is developed to study chemical reactions coupled with long-range mechanical phenomena in materials. The finite-element method for continuum mechanics is coupled with the molecular dynamics method for an atomic system that embeds a cluster of atoms described quantum-mechanically with the electronic density-functional method based on real-space multigrids. The hybrid simulation approach is implemented on parallel computers using both task and spatial decompositions. Additive hybridization and unified finite-element/molecular-dynamics schemes allow scalable parallel implementation and rapid code development, respectively. A hybrid simulation of oxidation of Si(111) surface demonstrates seamless coupling of the continuum region with the classical and the quantum atomic regions. © 2001 Elsevier Science B.V. All rights reserved.

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1. Introduction

In recent years, various forms of nanostructured materials [1,2] such as nanoparticles, thin films, and nanophase materials have attracted much attention due to their improved mechanical, catalytic, and opto-electronic properties [3] resulting from their nanometer-size domains [1,3]. Understanding formation dynamics of nanostructured materials and their resulting unique physico-chemical properties requires accurate dynamic simulations of chemically reacting atoms in these materials. Highly accurate simulations based on energy density-functional theory (DFT) [4,5] for electronic structures have been used extensively to study chemical reactions in clusters

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of atoms [6]. Despite considerable progress in formulation, algorithms, and parallel computing techniques, DFT-based dynamic simulations are currently limited to systems containing less than a few hundred atoms due to long computation times [7,8]. To overcome this limitation, we have recently developed a hybrid quantum-mechanical/molecular-dynamics (QM/MD) approach [9] to dynamic simulation of materials on parallel computers. The approach follows the idea on which hybrid quantum-mechanical/molecular-mechanics (QM/MM) methods [10–18] for geometrical optimization of large biological molecules are based: Computation can be made less when we partition a simulation system into different regions that are modeled with varying degrees of approximation. In the hybrid QM/MD approach, a QM system described by DFT based on real-space multigrids [8,9,19–24] is embedded in a classical system of atoms interacting via an empirical interatomic potential. Handshake atoms are introduced to couple the quantum and the classical systems dynamically based on the scaled position method [9]. The hybrid QM/MD approach enables dynamic simulations of material processes involving chemical reactions such as oxidation [9].

There is growing demand for large-scale materials simulations involving chemical reactions, e.g., to study the interplay between stress fields and chemical reactions. Stress in materials is long-ranged; it decays in proportion to the inverse-square-root of the distance from a crack [2,3]. Stress fields, which depend on the size and the overall shape of the system, may affect local atomic diffusion rates and hence chemical reactions. There are attempts to fabricate three-dimensional patterns in opto-electronic devices by controlling local atomic-diffusion and oxidation rates through stress [25–28]. Large-scale dynamic simulations with realistic stress fields are expected to play a key role in understanding atomistic mechanisms of these processes. Another example that requires large-scale simulations involving chemical reactions deals with micro-electro-mechanical systems (MEMS) [29], in which feature sizes are submicrons. Constitutive relations and scaling laws [2] in engineering mechanics have not been validated at such small length scales, and consequently lifetime prediction of MEMS is currently impractical [29]. Large-scale simulations involving chemical reactions will contribute significantly in this area by providing atomistic understanding of environmental effects on fracture and fatigue processes in MEMS.

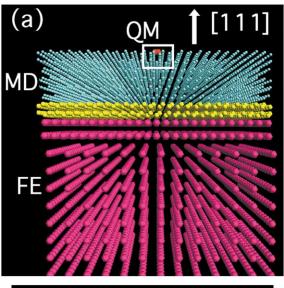
Recent advances in algorithms and parallel computers have enabled MD simulations [30] involving 10^8-10^9 atoms with system sizes exceeding 0.1 μ m [31,32]. With the hybrid QM/MD approach [9], systems with similar sizes can be simulated in which 10^3-10^4 atoms are treated quantum-mechanically, using scalable DFT algorithms [8]. To simulate entire MEMS and device structures (> 1 μ m), however, it is necessary to coarse-grain atomic details in the peripheral region of the system. The coarse-graining can be achieved with the finite element (FE) method [33], in which a material is regarded as a continuum and is decomposed into a mesh of finite elements.

Various handshake schemes have been proposed to couple the MD and the FE regions in hybrid FE/MD simulations [34–39]. In one of the first attempts by Mullins and Dokainish [34], pseudo-atoms embedded in finite elements interact with the MD atoms through the MD interatomic potential. Kohlhoff, Gumbsch, and Fischmeister [35] introduced a transition zone between the FE and the MD regions and scaled down the finite-element size to the atomic scale in the transition zone. Abraham et al. [36] further improved the FE/MD coupling by constructing an explicit Hamiltonian for the atoms and the FE nodes in the transition zone as an average of the MD and the FE Hamiltonians. The FE/MD approach has been applied to crack propagation in Si, in which QM calculations based on the semi-empirical tight-binding method are coupled with the MD and the FE methods [36, 37]. Lidorikis et al. [38] have extended the FE/MD approach and used it to study atomistically-induced stresses in Si/Si_3N_4 nanopixels.

In this paper, we develop a hybrid FE/MD/QM approach to materials simulations on parallel computers by combining the FE method with our hybrid QM/MD method [9] based on the FE/MD coupling scheme in Refs. [36–38]. Seamless coupling between the FE, MD and QM regions is demonstrated through a simulation run of oxidation of Si(111) surface. Sections 2 and 3 describe the present hybrid FE/MD/QM approach and its implementation on parallel computers, respectively. The parallel code is applied to oxidation of Si(111) surface in Section 4, and concluding remarks are given in Section 5.

2. Hybrid simulation scheme

In describing the present hybrid scheme, it is helpful to use the initial configuration of the hybrid simulation of oxidation of Si(111) surface (see Section 4). Fig. 1(a) shows the decomposition of the system into FE, MD, and QM regions. The system is periodic in two horizontal directions, while free boundary conditions are applied in the vertical direction, i.e. [111]. In the FE method, the system is regarded as a continuum and is decomposed into a mesh of finite elements. In Fig. 1(a), the FE mesh points (nodes) are plotted as magenta spheres, whereas the atoms are depicted as blue spheres. In the handshake (HS) region between the FE and the MD regions, the FE mesh is



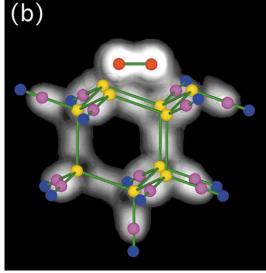


Fig. 1. (a) Initial configuration of the hybrid simulation of oxidation of Si(111) surface. Magenta spheres represent FE nodes; yellow, FE/MD-HS atoms; blue, MD atoms; red, O atoms. (b) Close up view of the QM and the QM/MD-HS atoms. Yellow spheres represent Si atoms; red, O atoms; blue, handshake Si atoms; magenta, termination H atoms. Charge densities are shown in grayscale.

refined down to the atomic scale in such a way that each FE node coincides with an MD atom [36–40]; yellow spheres in Fig. 1(a) represent these composite atoms/nodes constituting the FE/MD-HS region. The FE calculations apply to the FE and the FE/MD-HS regions, whereas the MD calculations apply to the MD and the FE/MD-HS regions. Red spheres above the top Si(111) layer in Fig. 1(a) represent an O₂ molecule. Fig. 1(b) shows the QM atoms as well as the HS atoms between the QM and the MD regions for the DFT calculations: red (O) and yellow (Si) spheres are the QM atoms, and blue spheres bonding to the yellow spheres represent the QM/MD-HS atoms. Magenta spheres in Fig. 1(b) correspond to virtual hydrogen atoms introduced in the DFT calculations to terminate dangling bonds of the QM atoms. Details of the termination scheme are described in Section 2.2.

Fig. 2 shows two-dimensional views of the FE/MD-HS region and its surroundings from two different directions. Hatched polygons with dots (nodes) at their corners or on their edges represent the finite elements. The finite elements, which are either prismatic or rectangular, occupy the whole FE and FE/MD-HS regions by sharing their corners or edges [38]. Total number of nodes in the finite element varies between 8 and 20 [38]. Twenty-node elements are used in the FE region far from the FE/MD-HS region, while eight-node elements are used close to the FE/MD-HS region. Side length of the finite element scales down to the atomic spacing in the FE/MD-HS region.

We denote positions of the FE nodes, MD atoms, and QM atoms as $\{\vec{r}_{FE}(i)\}, \{\vec{r}_{MD}(i)\}$, and $\{\vec{r}_{QM}(i)\}$, respectively. Similarly, $\{\vec{r}_{FE/MD}^{HS}(i)\}$ represents the FE/MD-HS atoms, and $\{\vec{r}_{QM/MD}^{HS}(i)\}$ the QM/MD-HS atoms. The dynamics of the system is determined by the Hamiltonian

$$H = H_{\mathrm{FE/MD}}^{\mathrm{system}}(\vec{R}_{\mathrm{all}}, \dot{\vec{R}}_{\mathrm{all}}) + E_{\mathrm{QM}}^{\mathrm{cluster}}\left(\{\vec{r}_{\mathrm{QM}}\}, \{\vec{r}_{\mathrm{QM/MD}}^{\mathrm{HS}}\}\right) - E_{\mathrm{MD}}^{\mathrm{cluster}}\left(\{\vec{r}_{\mathrm{QM}}\}, \{\vec{r}_{\mathrm{QM/MD}}^{\mathrm{HS}}\}\right) \tag{1}$$

where $\vec{R}_{all} = \{\{\vec{r}_{MD}\}, \{\vec{r}_{FE}\}, \{\vec{r}_{QM}\}, \{\vec{r}_{FE/MD}^{HS}\}, \{\vec{r}_{QM/MD}^{HS}\}\}$ and $\dot{\vec{R}}_{all} = d\vec{R}_{all}/dt$.

 $H_{\text{FE/MD}}^{\text{system}}$ in Eq. (1) is the FE/MD Hamiltonian (see Section 2.1) of the total system (including the FE, MD, and QM regions). The last two terms on the right hand side of Eq. (1) represent the QM correction to the MD potential energy for the cluster of atoms in the QM region [9,15,16]. The gradient of H with respect to the position $\vec{r_i}$ of the ith atom gives the force $\vec{F_i}$ on the atom as a summation of three partial forces corresponding to the three terms of

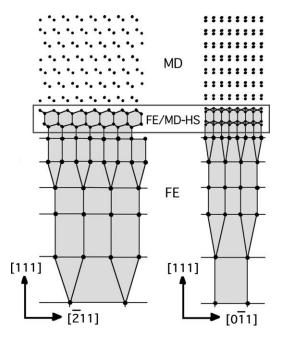


Fig. 2. Two-dimensional projections of the FE/MD-HS region and its surroundings in two different directions. The MD atoms and the FE nodes are plotted as dots. The finite elements are depicted as hatched polygons.

H in Eq. (1): $\vec{F_i} = -\partial H/\partial \vec{r_i} = \vec{F}_{\mathrm{FE/MD},i}^{\mathrm{system}} + \vec{F}_{\mathrm{QM},i}^{\mathrm{cluster}} - \vec{F}_{\mathrm{MD},i}^{\mathrm{cluster}}$. We note that $\vec{F}_{\mathrm{QM},i}^{\mathrm{cluster}} = \vec{F}_{\mathrm{MD},i}^{\mathrm{cluster}} = 0$ for those atoms which are neither the QM nor QM/MD-HS atoms

2.1. Coupling FE with MD

Following linear elasticity theory for continua, we may write the potential energy of the finite elements as [33]

$$\sum_{m} \int_{\text{element}(m)} d\vec{r} \frac{1}{2} \sum_{i,j,k,l}^{3} \varepsilon_{ij}(\vec{r}) C_{ijkl} \varepsilon_{kl}(\vec{r})$$
(2)

with the strain tensor field given by

$$\varepsilon_{ij}(\vec{r}) = \frac{\partial u_i(\vec{r})}{\partial r_i} + \frac{\partial u_j(\vec{r})}{\partial r_i},\tag{3}$$

where $\vec{u}(\vec{r})$ is the displacement field and the elastic matrix C_{ijkl} of the material is either obtained experimentally or calculated theoretically. We perform each integral in Eq. (2) by interpolating $\vec{u}(\vec{r})$ between the FE nodes using a linear (for the 8-node elements) or quadratic (for the 20-node elements) function of \vec{r} [33]. Denoting the total number of FE nodes for element-l as $n_{\text{node}}(l)$, Eq. (2) reduces to

$$\sum_{l}^{\text{elements}} \sum_{\mu,\nu}^{n_{\text{node}}(l)} \frac{1}{2} \vec{u}_{\mu} \cdot \overset{\leftrightarrow}{K}^{l}_{\mu,\nu} \cdot \vec{u}_{\nu}, \tag{4}$$

where $\vec{K}_{\mu,\nu}^l$ is the stiffness matrix [33] for element-l. We employ the lumped-mass approximation [33,38,40] for the kinetic energy of the finite elements, i.e. each FE node-a is assigned a mass m_a calculated with the mass density ρ_{mass} of the material:

$$m_a = \sum_{l}^{\text{elements } n_{\text{node}}(l)} \rho_{\text{mass}} V_l \delta_{a,i} / n_{\text{node}}(l),$$

where V_l is the volume of element-l, and $\delta_{a,i} = 1$ if node-a coincides with node-i of element-l and $\delta_{a,i} = 0$ otherwise. The FE mass reduces to the atomic mass m_i in the FE/MD-HS region.

We consider MD interatomic potentials that are composed of two-body $(\phi_2(i,j))$ and three-body $(\phi_3(i,j,k))$ terms as in Stillinger–Weber (SW) potential [41] for Si. To link the FE and the MD regions in a seamless manner, we introduce a weight function w for the MD atoms and the FE nodes [36–38]. We assign w=1 for the MD atoms in the MD region, and w=0 for the FE nodes in the FE region. In the FE/MD-HS region, all MD atoms in an atomic layer are assigned a single w value, and the value of w varies from 1 to 0 layer-by-layer in a stepwise manner. Similarly, w for the FE nodes in the FE/MD-HS region is graded element-by-element. Using the weight function, $H_{\text{FE/MD}}^{\text{system}}$ in Eq. (1) is written as

$$H_{\text{FE/MD}}^{\text{system}} = \sum_{i}^{\text{atoms\&elements}} \frac{1}{2} m_i v_i^2 + \frac{1}{2!} \sum_{i,j}^{\text{atoms}} w(i) \phi_2(i,j) + \frac{1}{3!} \sum_{i,j,k}^{\text{atoms}} w(i) \phi_3(i,j,k)$$

$$+ \frac{1}{2!} \sum_{l}^{\text{elements}} \sum_{\mu,\nu}^{n_{\text{node}}(l)} [1 - w(\mu)] \vec{u}_{\mu} \cdot \vec{K}_{\mu,\nu}^l \cdot \vec{u}_{\nu}, \qquad (5)$$

where $\{\vec{v}_i\}$ are velocities of the atoms and the FE nodes.

2.2. Coupling DFT with MD

An atomic cluster to be treated quantum-mechanically using the DFT is selected in the system, as depicted by red (O) and yellow (Si) spheres in Fig. 1(b). We consider an insulator such as ceramics or semiconductors, whose bonding pairs are known. Stabilizing atomic configuration of the cluster requires termination of its dangling bonds by hydrogen (H) atoms. The positions of the termination H atoms are determined from those of the QM/MD-HS atoms (blue spheres in Fig. 1(b)) as follows. Let $\vec{r}_{j(i)}$ and $n_c(i)$ be the positions of the QM atoms bonding to a QM/MD-HS atom at \vec{r}_i and the number of different j for each i, respectively. A termination H is placed at $\vec{x}_{i,j}^H = \beta \vec{r}_i + (1-\beta) \vec{r}_{j(i)}$ for each (i,j) pair with a control parameter β [9]. The DFT calculations of the H-terminated atomic cluster are performed with free boundary conditions to obtain $E_{\rm QM}^{\rm cluster}$ and the corresponding forces on the QM and the QM/MD-HS atoms. Value of β is determined to minimize mean square displacements of the QM atoms caused by cluster formation. In the oxidation simulation of Si(111) surface in Section 4, we choose $\beta = 0.625$.

In the Kohn–Sham (KS) formulation of DFT [4–6], total energy of a cluster of atoms located at $\{\vec{r}_k\}$ is written as

$$E_{\text{QM}}^{\text{cluster}}(\{\vec{r}_{k}\}) = 2\sum_{i=1}^{\text{occ}} \psi_{i}^{*} \left(-\frac{\nabla^{2}}{2}\right) \psi_{i} \, d\vec{x} + \frac{1}{2} \iint \frac{\rho(\vec{x})\rho(\vec{x}')}{|\vec{x} - \vec{x}'|} \, d\vec{x} \, d\vec{x}' + \int V_{\text{ion}}(\vec{x})\rho(\vec{x}) \, d\vec{x} + E_{\text{xc}}(\rho) + E_{\text{ion}}(\{\vec{r}_{k}\})$$
(6)

with the KS electronic wave functions $\{\psi_i\}$ and the charge density $\rho(x) = 2\sum_{i=1}^{\text{occ}} |\psi_i(\vec{x})|^2$. Atomic units are used in Eq. (6) and only doubly occupied states are considered. The KS wave functions obey the orthonormality constraint: $\int \psi_i^* \psi_j \, d\vec{x} = \delta_{ij}$. The V_{ion} in Eq. (6) is the pseudopotential for valence electrons; E_{xc} and E_{ion} are the exchange-correlation energy and the interaction energy between ion cores, respectively [4–6]. We may obtain $\{\psi_i\}$ as solutions to the following nonlinear differential equations [5–7]:

$$\left[-\frac{\nabla^2}{2} + V_{\text{ion}}(\vec{x}) + V_{\text{Hartree}}(\vec{x}) + \frac{\delta E_{\text{xc}}}{\delta \rho(\vec{x})} \right] \psi_i = e_i \psi_i$$
 (7)

with the Hartree potential $V_{\text{Hartree}}(\vec{x}) = \int \rho(\vec{x}')/|\vec{x} - \vec{x}'| d\vec{x}'$.

We use real-space multigrids for DFT calculations [8,9,22–24], in which $\{\psi_i\}$ and V_{Hartree} are represented on a uniform real-space mesh in Cartesian coordinates with an auxiliary set of coarser meshes. Details of the method are explained in Refs. [8,9]. We use norm-conserving pseudopotentials [42] for V_{ion} with the generalized gradient correction [43]. The second derivative of $\{\psi_i\}$ in Eqs. (6) and (7) is calculated by the sixth-order finite difference method [19–21]. The $\{\psi_i\}$ are solved by repeating the self-consistent field (SCF) iteration cycle [8,9,44]. Denoting ρ_{old} and $\{\psi_{i,\text{old}}\}$ as input charge density and wave functions, we may summarize the SCF cycle as the following five steps:

- (i) Iterative solution to the Poisson equation $\nabla^2 V_{\text{Hartree}}(\vec{x}) = -4\pi \rho_{\text{old}}(\vec{x})$;
- (ii) unitary transformation of $\{\psi_{i,\text{old}}\}$ to diagonalize the corresponding Hamiltonian matrix;
- (iii) conjugate-gradient [45] solutions $\{\psi_{i,\text{new}}\}$ to Eq. (7) with a preconditioning scheme [8,9], in which $\{\tilde{\psi}_{i,\text{old}}\}$ are used as initial values;
- (iv) estimation of improved charge density ρ_{new} by mixing ρ_{old} with $2\sum_{i=1}^{\text{occ}} |\psi_{i,\text{new}}|^2$ by the Pulay scheme [44]; and
- (v) orthonormalization of $\{\psi_{i,\text{new}}\}$ with the Gram–Schmidt method [45].

Convergence of both the Poisson equation in step (i) and Eq. (7) in step (iii) is accelerated with the multigrid method introduced originally by Brandt [46]. In the multigrid acceleration for Eq. (7), $V_{\text{ion}}(\vec{x}) + V_{\text{Hartree}}(\vec{x}) + \delta E_{\text{xc}}/\delta \rho(\vec{x})$ is fixed to ignore nonlinear coupling of the wave functions and eigenvalues [8,9,45].

For the calculations of $E_{\text{MD}}^{\text{cluster}}$ in Eq. (1), we similarly introduce classical termination atoms by displacing the QM/MD-HS atoms to minimize surface effects on atomic forces on the QM atoms [9]. Position $\vec{x}_{i,\{j\}}$ of the

termination atom-i is $\vec{x}_{i,\{j\}} = \alpha \vec{r}_i + (1 - \alpha) \langle \vec{r}_{j(i)} \rangle_j$, where α is a parameter and $\langle \cdots \rangle_j$ denotes taking average over different j. If a surface atom in the atomic cluster interacts only with its first nearest-neighbor atoms in the empirical interatomic potential, as in the SW potential for Si, we may set $\alpha = 1$. Value of $E_{\text{MD}}^{\text{cluster}}$ is obtained as the MD potential energy of the terminated atomic cluster.

3. Parallel hybrid simulation

The present hybrid approach is implemented on parallel computers using both task and spatial decompositions. Processors in a parallel computer are grouped into classical (CL) processors for FE and MD calculations and QM processors for DFT calculations (task decomposition). Taking advantage of the formal similarity in formula between the two-body MD interaction and the inter-node interaction between the FE nodes (see Eq. (5)), we modify an existing parallel MD code [31,32] such that it can also calculate the FE inter-node interaction. In this unified FE/MD code, particles are either FE nodes or MD atoms, and their positions and velocities are stored in common arrays. The linked cell lists [30] in the MD code are used to efficiently keep track of the element-node relations. The unified FE/MD algorithm is parallelized using spatial decomposition: The FE and MD regions are decomposed into sub-domains and mapped onto the CL processors [31,32]. The data associated with particles (either FE nodes or MD atoms) of a subsystem are assigned to the corresponding processor. To calculate the force on a particle in a subsystem, particle coordinates in the neighbor subsystems are "cached" from the corresponding processors. Particles that have moved out of a subsystem due to a time-stepping procedure are "migrated" to the proper destination processors. With the spatial decomposition, the computation time on a P-processor computer scales as N/P while communication scales in proportion to $(N/P)^{2/3}$ for an Nparticle system. The mesh points for discretizing the Hartree potential, V_{Hartree} , and the KS wave functions, $\{\psi_i\}$, for the DFT calculations are likewise decomposed and mapped onto the QM processors. The present parallel code is written in the single-program multiple-data programming style [47], which uses selection statements for the QM and the CL processors to execute only the corresponding code segments. The Message Passing Interface (MPI) [48] standard is used for data communication between the processors. To reduce the memory size required to run the code, dynamic allocation/deallocation operations in Fortran90 are applied to all the array variables [9].

At the start of a simulation, the hybrid code reads the stiffness matrices, $\hat{K}_{\mu,\nu}^l$, for all the elements in addition to the positions, velocities, and masses of the MD atoms and the FE nodes. Fig. 3 shows a flowchart of subsequent parallel computations:

- (i) the classical forces $\{\vec{F}_{\text{FE/MD}}^{\text{system}}\}$ for all the MD atoms and the FE nodes are calculated in the CL processors;
- (ii) atomic data for the QM and the QM/MD-HS atoms that are necessary to create an H-terminated cluster are transferred to the QM processors;
- (iii) the QM processors perform the DFT calculations to obtain QM forces $\{\vec{F}_{QM}^{cluster}\}$ for the QM and the QM/MD-HS atoms, while the CL processors calculate corresponding MD forces $\{\vec{F}_{MD}^{cluster}\}$ using the empirical interatomic potential;
- (iv) the QM forces are sent back to the CL processors; and, (v) the total forces $\{\vec{F}\} = \{\vec{F}_{FE/MD}^{system} + \vec{F}_{QM}^{cluster} \vec{F}_{MD}^{cluster}\}\$ are calculated in the CL processors, which in turn are used for time-integration of the equations of motion using the velocity-Verlet algorithm [30].

In our additive hybridization scheme, the total energy of the system is a linear combination of FE/MD and QM energies. Consequently the CL and the QM subtasks are executed independently except for the exchange of small messages containing species, coordinates, and QM forces for the cluster-atoms, as shown in the flowchart in Fig. 3. This modularity makes the present parallel implementation highly scalable, in contrast to multiplicative hybridization schemes that couple CL and QM tasks inseparably.

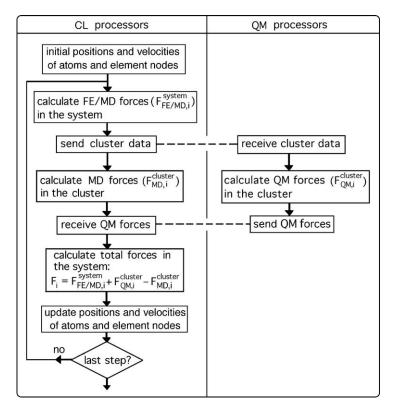


Fig. 3. A flowchart of parallel computations in the hybrid simulation code.

4. Demonstration of hybrid simulation on a parallel computer

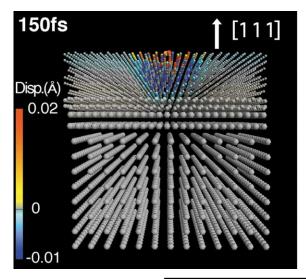
The parallel hybrid simulation code is applied to oxidation of Si(111) surface to demonstrate seamless coupling of the FE, MD, and QM regions. Understanding mechanisms of Si oxidation is crucial in successful design of MEMS and electronic devices [25–29]. Characteristic energy released in chemical reactions of an O₂ molecule with a Si surface is on the order of 1 eV [49–52]. The reaction energy as well as associated stress and strain are transferred to the surrounding atoms and may substantially affect subsequent dynamic processes. It is thus important that dynamic simulations of oxidation include a large environmental region in addition to reacting atoms.

For the hybrid simulation, a slab with dimensions (212.8, 245.7, 83.1 Å) in ([211], [011], [111]) directions is cut out from bulk Si. The MD and the FE/MD-HS regions consist of 12 and 4 atomic layers along [111] direction, respectively, whereas the FE region corresponds to bottom two-thirds of the Si slab (see Fig. 1(a)). Periodic boundary conditions are applied in [$\bar{2}11$] and [$\bar{0}11$] directions. The total number of atoms and FE nodes for the Si slab is N=15,212. The elastic matrix elements of Si at zero temperature are obtained using the SW potential with mass density $\rho_{\text{mass}}=2.35 \text{ g/cm}^3$ [53].

Initial configuration of the hybrid simulation is obtained by placing an O_2 molecule (oriented along [$\bar{2}11$] direction with zero velocity) 2.0 Å above the (111) surface of the slab. Total number of atoms treated in the DFT calculations is 25 that includes 10 Si atoms, 2 O atoms, and 13 H atoms for termination, see Fig. 1(b). Initial charge densities of the terminated atomic cluster obtained in the DFT calculations are also shown in grayscale in Fig. 1(b). Neither QM/MD-HS nor MD atoms are found within the interaction ranges of the O atoms during the present simulation. Accordingly the MD interatomic potentials for O–O and Si–O pairs may be arbitrary, since the potential energies for O–O and Si–O pairs in $E_{\rm MD}^{\rm cluster}$ cancel with corresponding terms in $H_{\rm FE/MD}^{\rm system}$ in Eq. (1).

We have performed the hybrid simulation for 1000 fs using 9 processors (550 MHz Intel Pentium III) on a PC cluster interconnected with Fast Ethernet switches; 8 processors are assigned to the QM calculations. The MD time step is 1.0 fs, and the finest mesh spacing of the real-space multigrids in the DFT calculations is 0.26 Å. Wall-clock time per MD step is 15 min, 99% of which is spent for the electronic-structure calculations in the QM processors. A single self-consistent field cycle in the DFT takes 130 s in total including 20 s for data communication between the QM processors.

Fig. 4 shows snapshots of the atomic configuration at 150, 300, and 900 fs, in which [111] displacements of the atoms and the FE nodes are color-coded. The O₂ molecule dissociates and each O atom is captured by a Si–Si bond at the surface to form a Si–O–Si structure, which is associated with increase in the Si–Si distance. Resulting strains in the QM region are transferred to the surrounding Si atoms in the MD region as shown in Fig. 4. Such strain



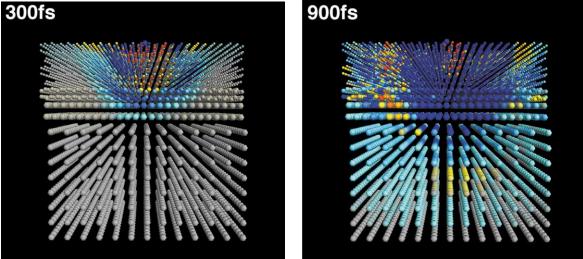


Fig. 4. Snapshots at 150, 300, and 900 fs in the hybrid simulation of oxidation of Si(111) surface. Colors represent [111]-displacements of the atoms and the FE nodes.

waves reach the QM/MD-HS region at \sim 300 fs, and propagate into the FE region at \sim 900 fs with no reflection or refraction observed at the QM/MD and MD/FE boundaries.

To analyze the transfer of kinetic energy, we partition the total system into slices along the [111] direction and calculate the kinetic energy of the atoms and the FE nodes in each slice. Fig. 5 shows time evolution of the kinetic energies in the slices; Z denotes the coordinate along the [111] axis and Z_{surf} corresponds to the position of the top Si-layer. The four vertical lines around $Z_{surf} - Z \approx 5$ Å in Fig. 5 represent the positions of the QM/MD-HS atoms; the positions of the FE/MD-HS atoms are bounded by the two vertical lines at $Z_{surf} - Z = 19.3$ and 23.3 Å. In Fig. 5, the kinetic energy varies smoothly as a function of Z at all times, indicating seamless coupling of the FE, MD, and QM regions.

The total energy, H, in Eq. (1) is a conserved quantity in the present hybrid scheme. Fig. 6 compares time evolution of $H_{\rm FE/MD}^{\rm system}/N$ and H/N. While $H_{\rm FE/MD}^{\rm system}/N$ changes by 2×10^{-5} eV during 200–260 fs, H/N conserves

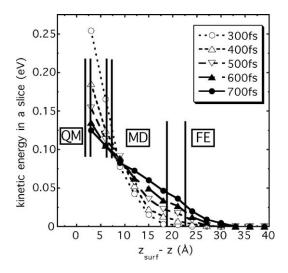


Fig. 5. Time evolution of kinetic energies in slices. Z is the position of a slice in [111]-axis; Z_{surf} , position of the surface atomic layer. The four vertical lines around $Z_{surf} - Z \approx 5$ Å represent the QM/MD-HS atoms; the FE/MD-HS atoms are bounded by the two vertical lines at $Z_{surf} - Z = 19.3$ and 23.3 Å.

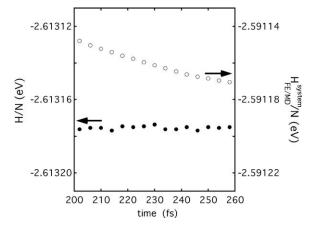


Fig. 6. Time evolution of $H_{\rm FE/MD}^{\rm system}/N$ and H/N. N is the total number of atoms and FE nodes.

well with fluctuations of 2×10^{-6} eV. Such an accurate conservation of the total energy is necessary to study heat transfer from the QM region to the MD and FE regions.

5. Concluding remarks

We have developed a hybrid FE/MD/QM simulation approach by coupling the FE method for a continuum with the MD method for atomistic simulations and the real-space multigrid-based DFT for QM calculations. We have performed a hybrid simulation of oxidation of Si(111) surface to demonstrate seamless coupling of the FE, MD, and QM regions. The present hybridization approach embeds a single QM cluster in a MD simulation, but an extension to include multiple QM clusters described by various approximation methods such as the tight-binding method is straightforward. Our parallel FE/MD/QM algorithm based on the modular, additive hybridization scheme requires little data communication between the CL and the QM processors, and accordingly, it can be implemented efficiently on a set of loosely-coupled computer clusters with low inter-cluster data transfer rates, by assigning the CL and the QM tasks to different computer clusters. Such hybrid simulations in "Grid"-computing environments [54,55] are in progress.

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